

[CONTRIBUTION FROM THE CHEMICAL LABORATORY OF NORTHWESTERN UNIVERSITY]

**Magnetic Susceptibilities of  $\text{Cr}_2\text{O}_3\text{-Al}_2\text{O}_3$  and of  $\text{Fe}_2\text{O}_3\text{-Al}_2\text{O}_3$  Solid Solutions**

BY P. W. SELWOOD, LORRAINE LYON AND MARYLINN ELLIS

Magnetic susceptibility measurements from 90 to 300°K. have been made for the solid solutions  $\text{Cr}_2\text{O}_3\text{-Al}_2\text{O}_3$  and  $\text{Fe}_2\text{O}_3\text{-Al}_2\text{O}_3$ . At infinite magnetic dilution the  $\text{Cr}^{+3}$  ion has a magnetic moment of 3.8 Bohr magnetons. The Weiss constant is zero. The  $\text{Fe}^{+3}$  ion under similar conditions has a moment of 5.9 and a Weiss constant of zero. The moment of the  $\text{Fe}^{+3}$  ions decreases rapidly with increasing magnetic concentration. These results tend to favor conclusions previously reached concerning the structure of supported iron sesquioxide on high area alumina, and the structure of hydrous iron sesquioxide and of transition group oxide supported catalysts and gels in general.<sup>1</sup>

Previous papers from this Laboratory have shown that the iron in supported iron sesquioxide has a magnetic moment of 4.0 to 4.4 Bohr magnetons, instead of the expected 5.9 magnetons predicted by the spin-only formula for the five unpaired electrons supposed to exist in the  $\text{Fe}^{+3}$  ion.<sup>2</sup> The subnormal moment also occurs in hydrous, or gel-like, iron sesquioxide.<sup>3</sup> This effect has been considered<sup>4</sup> to be due to some degree of wave function overlapping between adjacent iron ions in accordance with the suggestion of Haraldsen and Klemm<sup>5</sup> of covalent bonds between adjacent positive paramagnetic ions. Some significance has been attached to this in the interpretation given previously for the magnetic properties of disperse transition group oxides in relation to the paramagnetic neighborhood. The reasoning involved will be reviewed briefly.

In terms of exchange interaction the Weiss constant is  $\Delta = 2JzS(S+1)/3k$  where  $J$  is the exchange integral,  $z$  the number of nearest paramagnetic neighbors possessed by each paramagnetic ion,  $S$  the spin quantum number and  $k$  the Boltzmann constant. For oxides in the supported or gel-like forms such as chromia supported on alumina, or as chromia gel, the only structural difference between these disperse states and the massive (crystalline) state must reside in  $J$  or in  $z$ , or in both.

The problem of whether the structural difference between disperse and massive states resides in  $J$  or in  $z$  has not been resolved, but the low moment found for iron in the disperse forms of iron sesquioxide has been taken as evidence that  $J$  is not appreciably different in the crystalline pure sesquioxide and in the gel. It is known that  $J$  is dependent on the third power of the distance between adjacent iron ions. It was felt that if the minimum distance between adjacent iron ions is greater in the disperse state than in the massive state, then the exchange integral and hence both the Weiss constant and the magnetic moment would be very sensitive to this increase. Failure to find an increase of moment with increasing dispersion in dilute supported iron sesquioxide on alumina was, therefore, regarded as evidence that

(1) This is the ninth paper on the susceptibility isotherm from this Laboratory. The eighth, by Selwood and Lyon, appeared in *Discussions of the Faraday Society "Heterogeneous Catalysis,"* No. 8, 1950, p. 222.

(2) P. W. Selwood, M. Ellis and K. Wethington, *THIS JOURNAL*, **71**, 2181 (1949).

(3) P. W. Selwood, M. Ellis and C. F. Davis, Jr., *ibid.*, **72**, 3549 (1950).

(4) F. N. Hill and P. W. Selwood, *ibid.*, **71**, 2522 (1949).

(5) H. Haraldsen and W. Klemm, *Z. anorg. allgem. Chem.*, **220**, 183 (1934).

$z$  was the only quantity appreciably different in the two cases.

It is well known that magnetically dilute substances containing ionically bound (+3) iron show a normal, spin-only, moment of 5.9 to 6.0 magnetons. There is, nevertheless, the possibility that some kind of covalent bond may exist between iron and oxygen, leading to a subnormal moment in the several disperse forms of iron sesquioxide. A method for examination of this idea is to study the susceptibility of  $\text{Fe}^{+3}$  ions at effectively infinite magnetic dilution but with the iron-oxygen relation virtually unchanged. This may be done by preparing solid solutions of iron sesquioxide in alumina. The susceptibilities are then measured at several temperatures over a range of concentration sufficient to permit extrapolation to infinite magnetic dilution. The magnetic moment may thus be calculated for conditions where no exchange effects occur.

**Experimental Part**

**Preparation of  $\text{Cr}_2\text{O}_3\text{-Al}_2\text{O}_3$  Solid Solutions.**—Measured quantities of chromic nitrate and of aluminum nitrate analyzed stock solution were mixed and poured into excess dilute ammonium hydroxide solution. The coprecipitated mixture was diluted, filtered, dried at 110°, and calcined in hydrogen at 1100° for 3–5 hours. The products ranged from ruby-pink at the low chromia end to green at the high chromia end. Homogeneity was established by X-ray studies on all samples. No further change of X-ray pattern occurred on longer calcination. The oxides formed were, of course, those corresponding to alpha alumina. Two or three samples gave evidence of slight ferromagnetism. These were discarded.

**Preparation of  $\text{Fe}_2\text{O}_3\text{-Al}_2\text{O}_3$  Solid Solutions.**—The method used for these solutions was parallel to that described for chromia-alumina. Several of the samples became ferromagnetic as revealed by a slight field strength dependence of susceptibility. These were discarded.

**Experimental Methods.**—All X-ray and some magnetic measurements were made as described in earlier papers from this Laboratory. Most of the magnetic measurements were made on a Faraday balance to be described later.

**Results**

Results on the  $\text{Cr}_2\text{O}_3\text{-Al}_2\text{O}_3$  series are given in Table I. The quantity  $\chi$  is the magnetic susceptibility per gram of sample,  $\chi_{\text{Cr}}$  is the susceptibility per gram of chromium after corrections have been made for the diamagnetism of the oxide, aluminum and chromic ions.

Table II shows similar results on the  $\text{Fe}_2\text{O}_3\text{-Al}_2\text{O}_3$  series.

**Discussion of Results**

It will be noted that the susceptibilities of both chromium and of iron ions increase greatly with increasing dilution. This effect is so great that, for instance, the susceptibility per gram of sample

TABLE I

MAGNETIC DATA ON CHROMIA-ALUMINA SOLID SOLUTIONS

Cr <sub>2</sub> O <sub>3</sub> , %	Temp., °K.	$\chi \times 10^4$	$\chi_{Cr} \times 10^4$	Cr <sub>2</sub> O <sub>3</sub> , %	Temp., °K.	$\chi \times 10^4$	$\chi_{Cr} \times 10^4$	
2.6	300	1.7	113	33.0	300	15.0	67	
	230	2.3	153		230	18.4	82	
	215	2.5	165		215	19.3	87	
	200	2.6	174		200	20.1	89	
	184	3.1	189		184	21.5	96	
	148	4.0	248		167	23.0	102	
	128	4.2	259		128	30.0	133	
	84	6.8	405		43.0	300	16.8	58
	5.3	300	3.0			92	230	20.4
		230	4.4		131	215	20.4	70
184		5.5	161	200	21.8	75		
128		7.9	228	184	22.8	79		
82		12.3	318	167	24.3	84		
8.2	300	6.1	112	128	34.2	117		
	230	6.9	129	83	52.0	179		
	215	7.6	141	54.0	300	19.1	53	
	200	8.0	148		230	22.7	62	
	184	8.6	159	215	23.5	56		
	128	12.1	222	200	24.2	66		
	83	17.5	317	184	26.5	73		
	17.6	300	10.9	94	128	36.6	100	
230		13.4	114	83	47.0	129		
215		14.5	123	74.6	300	22.6	44	
200		15.2	129		230	25.7	51	
184		16.1	137	215	26.2	52		
167		17.3	147	200	26.3	52		
128		22.0	186	184	26.8	53		
84		27.9	235	167	27.2	54		
25.0		300	12.7	74	90	32.0	63	
		230	15.9	94	81.6	300	23.6	43
	215	17.2	102	230		26.3	48	
	200	17.8	105	215	27.0	49		
	184	18.5	109	200	27.2	49		
	128	23.6	140	184	27.6	50		
	83	33.8	198	90	29.5	53		

for the sample containing 43.0% chromia is actually twice as large, at liquid air temperature, as is the susceptibility of pure crystalline chromia at the same temperature. It will be noted also that the Curie-Weiss law describes the behavior of both Cr<sub>2</sub>O<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> and Fe<sub>2</sub>O<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> systems at moderate and low concentrations of the paramagnetic ions. For the lowest chromia concentration studied, 2.6% the Weiss constant is +4°, which is scarcely distinguishable from zero. The moment is 3.7, in good agreement with the spin-only value of 3.8. Extrapolation of the susceptibilities to infinite magnetic dilution yields a Weiss constant of zero and a moment of 3.8 magnetons. It should be mentioned that the low temperature susceptibility of chromia is quite sensitive to the presence of alumina in little more than trace amounts. This is probably a consequence of the ability of a diamagnetic ion present in effect as a lattice defect

TABLE II

MAGNETIC DATA ON FERRIC OXIDE-ALUMINA SOLID SOLUTIONS

Fe <sub>2</sub> O <sub>3</sub> , %	Temp., °K.	$\chi \times 10^4$	$\chi_{Fe} \times 10^4$	Fe <sub>2</sub> O <sub>3</sub> , %	Temp., °K.	$\chi \times 10^4$	$\chi_{Fe} \times 10^4$	
2.0	300	3.3	236	20.0	300	15.8	114	
	230	4.4	336		230	20.5	148	
	184	5.2	393		215	21.8	157	
	138	6.8	507		200	22.3	161	
	128	7.5	560		184	22.9	165	
	86	9.5	700		167	25.1	181	
	5.0	300	6.1		183	148	27.3	197
		230	7.8		232	128	31.0	223
		215	8.2		243	86	38.9	279
		200	9.1		268	40.0	300	17.7
184		9.9	291	230	20.0		72.1	
10.5	167	11.0	323	215	20.8	75.0		
	148	12.7	371	200	21.5	77.5		
	128	14.6	426	184	22.4	80.8		
	86	19.7	571	167	22.9	82.5		
	300	11.8	166	148	25.6	92.2		
	230	15.1	211	128	27.5	99.0		
	215	15.8	221	86	34.2	123		
	200	16.7	235	80	300	37.1	66.2	
	184	18.7	260		86	44.2	79.0	
	167	19.7	274	10.5	148	21.1	293	
128	25.0	340	86		32.5	450		

to unlock the antiparallel spins of all paramagnetic ions in its vicinity.

The extrapolated susceptibilities for the Fe<sup>+3</sup> ion at infinite dilution give a Weiss constant of zero and a moment of 5.9 magnetons. It is interesting to note the tenacity with which one iron ion seems attracted to another. Below 5% iron the Weiss constant is effectively zero, but the moment is changing rapidly with concentration. Thus at 1.4% iron the moment is 5.9; at 3.5% iron it is 5.0; while at 14% iron the moment is 4.3, with a Weiss constant in the last case of 52°.

The moment of the iron ions at infinite dilution supports the view previously expressed, namely, that the subnormal moment observed in the disperse systems containing iron sesquioxide is due to a species of covalent bond between adjacent iron ions. This in turn supports the view that the susceptibility isotherms shown by almost all transition group oxides owe their shape more to the quantity z, that is, the number of paramagnetic neighbors, and less to possible changes in the minimum iron-iron distance in the transition from crystalline massive oxide to amorphous gel-like oxide.

This work was supported by the Office of Naval Research and by the Signal Corps Engineering Laboratories